



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS						
<b>Predmet:</b>	<b>Fraktali in dinamični sistemi</b>					
<b>Course title:</b>	<b>Fractals and dynamical systems</b>					
<b>Študijski program in stopnja</b> Study programme and level	<b>Študijska smer</b> Study field			<b>Letnik</b> Academic year	<b>Semester</b> Semester	
Matematika, 2. stopnja				<b>1. ali 2.</b>	<b>1. ali 3.</b>	
Mathematics, 2 <sup>nd</sup> degree				<b>1. or 2.</b>	<b>1. or 3.</b>	
<b>Vrsta predmeta / Course type</b>				izbirni / elective		
<b>Univerzitetna koda predmeta / University course code:</b>						
<b>Predavanja</b> Lectures	<b>Seminar</b> Seminar	<b>Sem. vaje</b> Tutorial	<b>Lab. vaje</b> Laboratory work	<b>Teren. vaje</b> Field work	<b>Samost. delo</b> Individ. work	<b>ECTS</b>
45		15	15		135	7
<b>Nosilec predmeta / Lecturer:</b>		Mateja Grašič				
<b>Jeziki /</b> <b>Languages:</b>	<b>Predavanja / Lectures:</b>	SLOVENSKO/SLOVENE				
	<b>Vaje / Tutorial:</b>	SLOVENSKO/SLOVENE				
<b>Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:</b>				<b>Prerequisites:</b>		
Linearna algebra, Algebra, Analiza 2				Linear algebra, Algebra, Analysis 2		
<b>Vsebina:</b>				<b>Content (Syllabus outline):</b>		
<ul style="list-style-type: none"><li>• Metrični prostor, različne vrste podprostorov, prostor fraktalov.</li><li>• Afine transformacije, skrčitve, sistemi iterirajočih funkcij.</li><li>• Osnove dinamičnih sistemov, dinamika fraktalnih množic.</li><li>• Teoretično in eksperimentalno določanje dimenzije fraktala, Hausdorff-Bezikovičeva dimenzija.</li><li>• Juliajeve množice, primeri njihove uporabe.</li></ul>				<ul style="list-style-type: none"><li>• A metric space, different types of subspaces, the space of fractals.</li><li>• Affine transformations, contraction mappings, systems of iterating functions.</li><li>• Introduction to dynamical systems, dynamics on fractal sets.</li><li>• The theoretical and experimental determination of the fractal dimension, Hausdorff-Besicovitch dimension.</li><li>• Julia sets, examples of their application.</li></ul>		

**Temeljni literatura in viri / Readings:**

G. Edgar: Classics on Fractals. Westview Press, Boulder (1992).

K. J. Falconer: Fractal Geometry. J. Wiley, Chichester (1990).

Y. Pesin, V. Climenhaga: Lectures on Fractal Geometry and Dynamical Systems, American Mathematical Society (2009).

R. Devaney: An Introduction To Chaotic Dynamical Systems, 2nd ed., Westview Press (2003).

J. Vrabec: Metricni prostori. Ljubljana: DMFA (1993).

**Cilji in kompetence:**

Študenti se seznanijo s strukturo podprostora fraktalov v metričnem prostoru in z osnovnimi načini generiranja fraktalov (družine iterirajočih preslikav). Spoznajo tudi različne pristope k določanju dimenzije fraktala ter dinamiko fraktalnih množic.

**Objectives and competences:**

Students get familiar with the structure of the subset of fractals in a metric space and with the main ways of generating fractals (iterated functions systems). They also study different approaches to the fractal dimension and the dynamics of fractal sets.

**Predvideni študijski rezultati:**

Znanje in razumevanje:

- aktivno obvladanje strukture metričnega prostora in prepoznavanje fraktalnih podmnožic
- teoretično in eksperimentalno določanje dimenzije fraktalov
- analiza dinamičnih sistemov in njihova uporaba

Prenesljive/ključne spretnosti in drugi atributi:

- sposobnost generiranja fraktalov
- izračun dimenzije fraktalne množice
- modeliranje z dinamičnimi sistemi

**Intended learning outcomes:**

Knowledge and Understanding:

- active knowledge of metric space structure and the ability to recognize its fractal subsets
- theoretical and experimental ways for finding the dimension of a fractal
- the analysis of dynamical systems and their application

Transferable/Key Skills and other attributes:

- the ability to generate fractals
- the calculation of fractal dimension
- modeling with dynamical systems

**Metode poučevanja in učenja:**

- Predavanja
- Seminarske, laboratorijske vaje
- Individualno delo

**Learning and teaching methods:**

- Lectures
- Tutorial
- Individual work

**Načini ocenjevanja:****Assessment:**

Način (pisni izpit, ustno izpraševanje, naloge, projekt):	Delež (v %) / Weight (in %)	Type (examination, oral, coursework, project):
Seminarska naloga	20%	Seminar work
Pisni izpit – praktični del	40%	Written exam – practical part
Ustni izpit – teoretični del	40%	Oral exam – theoretical part
Pisni izpit – praktični del se lahko nadomesti z dvema delnima testoma (sprotni obveznosti).		Written exam – practical part can be replaced by two partial tests (mid-term testing).
Vsaka izmed naštetih obveznosti mora		Each of the mentioned commitments

biti opravljena s pozitivno oceno.

Opravljen pisni del izpita je pogoj za pristop k teoretičnem delu izpita.

must be assessed with a passing grade.

Passing grade of the written exam is required for taking the oral exam.

**Reference nosilca / Lecturer's references:**

1. BENKOVIČ, Dominik, GRAŠIČ, Mateja. Jordan  $\{g,h\}$ -derivations of unital algebras. *Operators and matrices*. 2022, vol. 16, no. 2, str. 415-428. ISSN 1846-3886. <http://oam.ele-math.com/16-32/Jordan-g,h-derivations-of-unital-algebras>, DOI: [10.7153/oam-2022-16-32](https://doi.org/10.7153/oam-2022-16-32). [COBISS.SI-ID [114972163](https://nbn-resolving.org/urn:nbn:si:coibiss-114972163)]

2. XIA, Yong-Hui, GRAŠIČ, Mateja, HUANG, Wentao, ROMANOVSKI, Valery. Limit cycles in a model of olfactory sensory neurons. *International journal of bifurcation and chaos in applied sciences and engineering*. 2019, vol. 29, no. 3, str. 1950038-1-1950038-9. ISSN 0218-1274. DOI: [10.1142/S021812741950038X](https://doi.org/10.1142/S021812741950038X). [COBISS.SI-ID [22250006](https://nbn-resolving.org/urn:nbn:si:coibiss-22250006)]

3. BENKOVIČ, Dominik, GRAŠIČ, Mateja. Generalized skew derivations on triangular algebras determined by action on zero products. *Communications in algebra*. 2018, vol. 46, iss. 5, str. 1859-1867. ISSN 0092-7872. <https://doi.org/10.1080/00927872.2017.1360334>, DOI: [10.1080/00927872.2017.1360334](https://doi.org/10.1080/00927872.2017.1360334). [COBISS.SI-ID [18505817](https://nbn-resolving.org/urn:nbn:si:coibiss-18505817)]